

University of Luxembourg

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## A Sustainable and Trustworthy AI Recommitment System (STAIRS)

As part of the STAREBEL project:  
“Toward A.I. Recommitment Strategies  
for ESG integration in Private Equity”



# Content



Context & motivation



Evolutionary Learning of Private Equity  
Recommitment Strategies



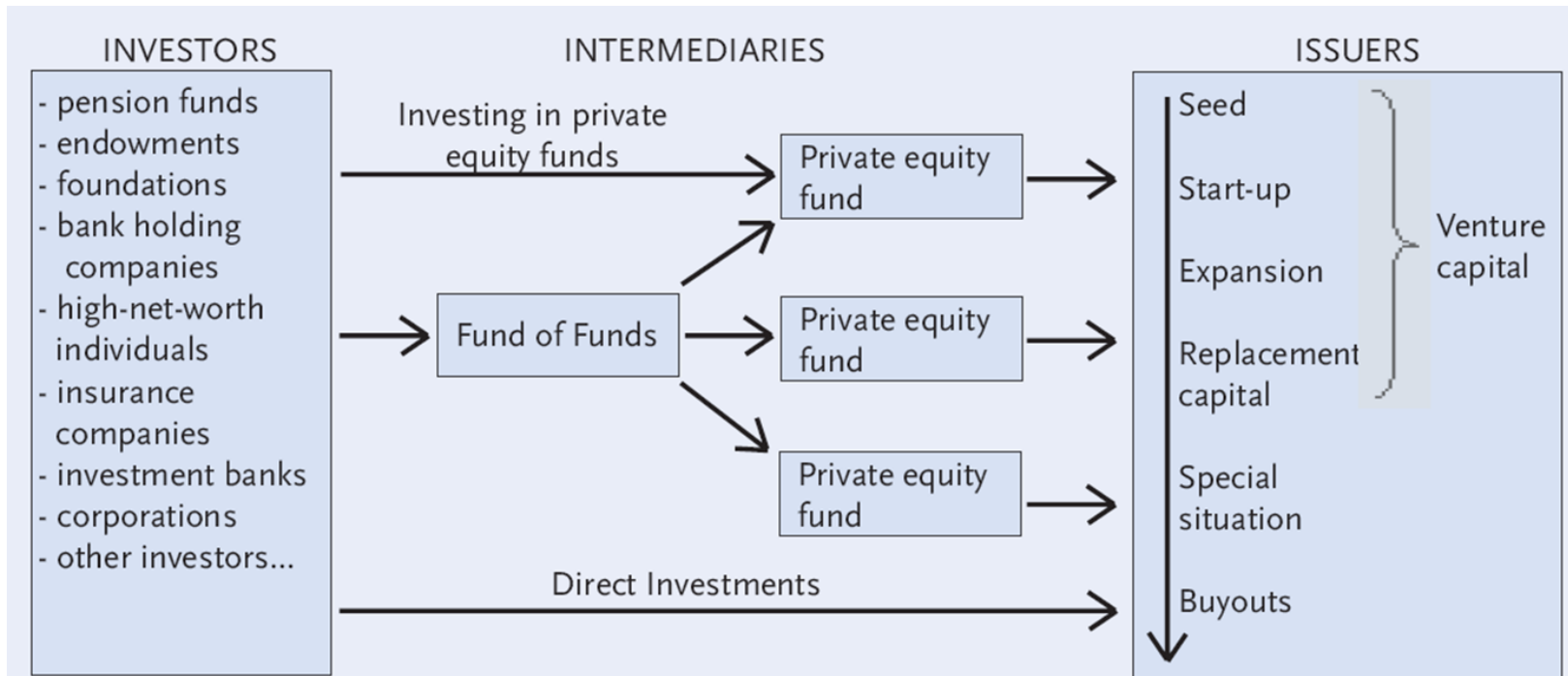
Proximal Policy Optimisation for a Private Equity  
Recommitment System



Conclusion & Perspectives

# Private Equity (PE)

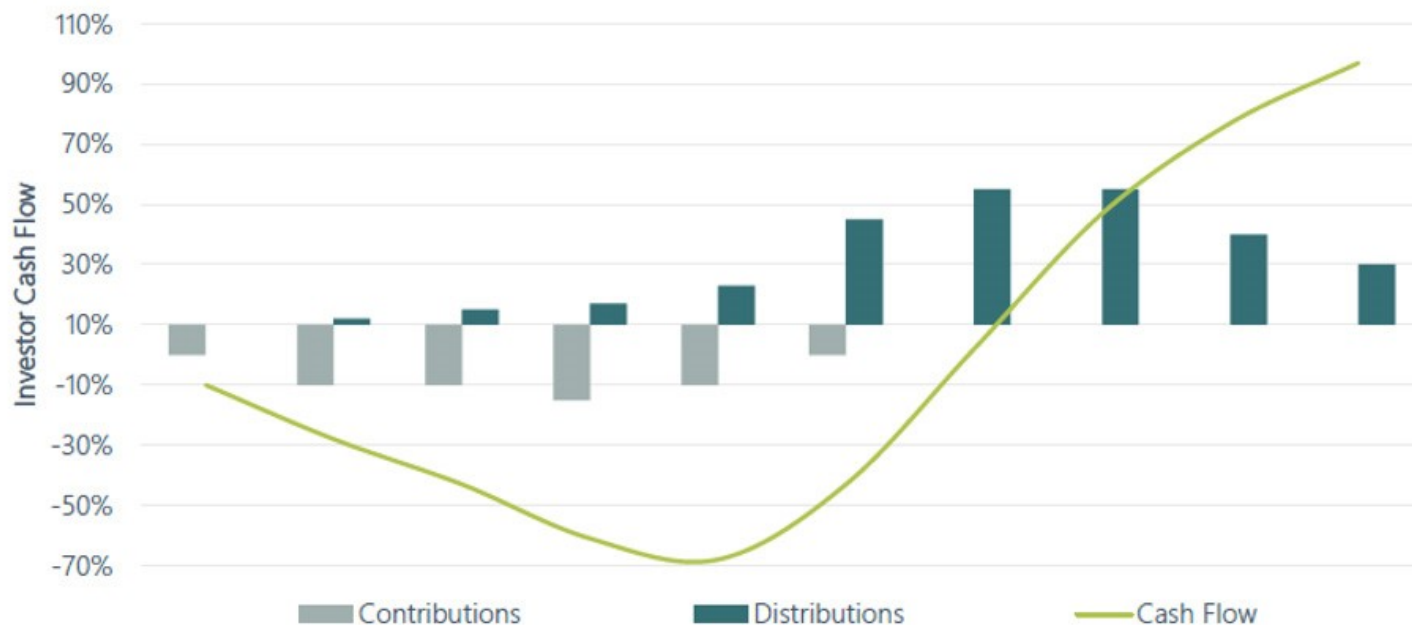
- Alternative investment class
- Has gained a great amount of influence in today's financial marketplace
- Included in the portfolio of sovereign wealth funds, pension funds ...



Source: Federal Reserve Bank of Dallas, IFSL, EVCA/Thomson Venture Economics/PricewaterhouseCoopers

# Private Equity Funds

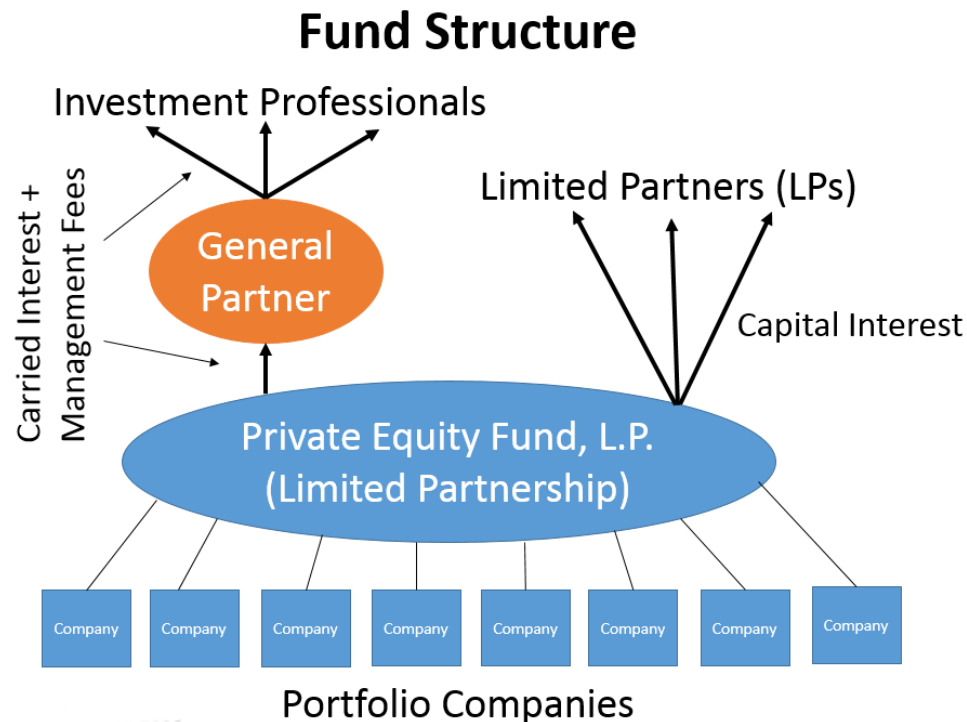
## Private Equity Fund – Cash Flow Model



Investment Stage	Development stage	Maturity/Liquidation stage
Year 1 through year 4-5, typically	Year 3 to year 8, typically	Year 8+, typically
<ul style="list-style-type: none"> <li>» Capital is committed and drawn down</li> <li>» Investments are made in portfolio companies</li> </ul>	<ul style="list-style-type: none"> <li>» Initial investment starts to mature</li> <li>» Mature investments are exited</li> <li>» Cash distributions are paid to investors</li> <li>» Follow-on investments are made</li> </ul>	<ul style="list-style-type: none"> <li>» Most investments have been exited</li> <li>» Several investments are left to "wind down"</li> </ul>

# Limited Partnership Funds

- Investing directly to companies requires high level of expertise, experience and staff incentives
- Institutional investors prefers to invest as Limited Partners
- LPs commit capital to the fund. General Partner (GP) calls the committed capital.



- Stakes in PE are illiquid due to restriction on sales
- Exposure to PE by investing in new funds in which they commit
- Capital is drawn down gradually over several years
- Very often Capital is not entirely called
- Payouts (distributions) occurrence vary between funds
- Most of these distributions cannot be reinvested immediately and are recommitted to new PE funds
- Consequently:
  - Cash inflows and outflows are uncertain
  - Investor have no control
  - Can lead to PE misallocation

# How to maintain high PE allocation

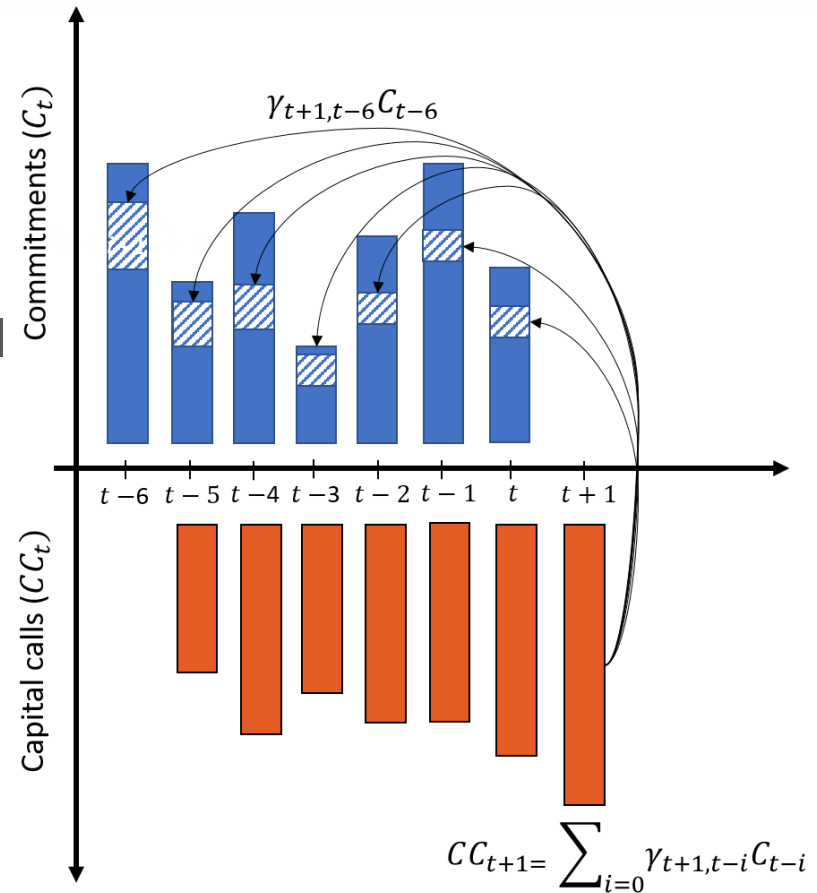
- **Underinvestment** because of undrawn Capital may lead to a drop of portfolio performance
- **Overinvestment** due to too large commitments may result in a liquidity shortfall
- Find a trade-off by keeping **investment degree** close to 1:
  - $ID_t = \frac{NAV_t}{NAV_t + Cash_t} \approx 1$  for all period t
  - A multi-period portfolio optimization
- Dynamic evolution of PE portfolio
- Need a strategy to be applied at each period t

# Solve multiple single-period portfolios

- Based on single-period portfolio optimization problem for each period  $t$
- $\min_{C_t} E_t(1 - ID_{t+1})^2$  with  $E_t$  the conditional expectation at end of period  $t$

- Analytical solution found at 
$$C_t = E_t \left( \frac{Cash_t + D_{t+1} - \sum \gamma_{t+1,i+1} C_{t-1}}{\gamma_{t+1,1}} \right)$$

- Involve data from period  $t+1$



with  $\gamma_{t+1,t-i}$ , the fraction of capital committed  $i$  periods ago and called at  $t + 1$



# Recommitment rules (deZwart 2012)

- “Private Equity Recommitment Strategies for Institutional Investors”

- Propose for the **Dutch Pension Fund (APG)**

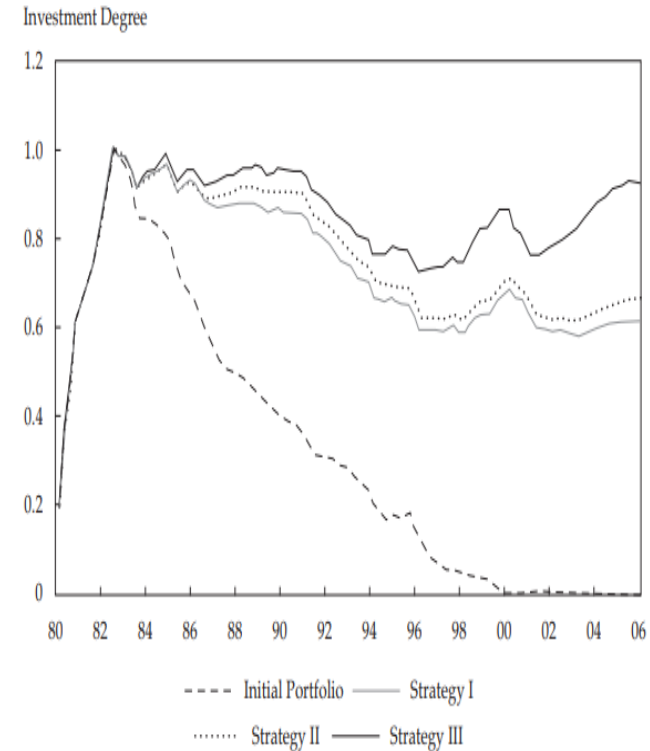
- No cashflow forecasting

- Manually designed rules of thumb as strategies:

- $DZ^1: C_t = D_t$

- $DZ^2 : C_t = D_t + UC_{t-p}$

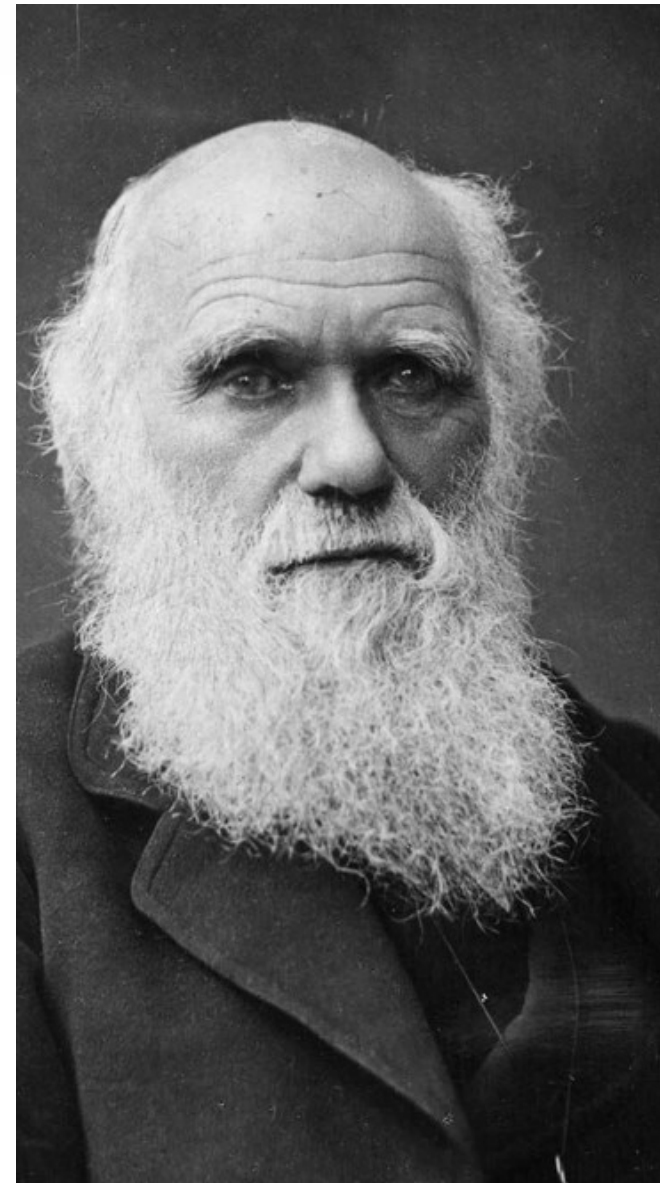
- $DZ^3 : C_t = \frac{1}{ID_t} (D_t + UC_{t-p})$



- Can we find better ones automatically ? Can we learn to optimize strategies ?

- With additional constraints, manually designed rules become unsuitable

# Evolutionary Learning of Private Equity Recommitment Strategies



- Search heuristic that is inspired by Charles Darwin's theory of natural evolution
- “**Individuals** with **traits** that enable them to **adapt** to their environments will help them survive and **have more offspring**, which will inherit those **traits**.”
- Technique of evolving programs
- Global Optimization approach:
  - Derivative-free
  - No assumption
- Evolving programs already mentioned by A.Turing (1950's)

Recommitment  
strategies

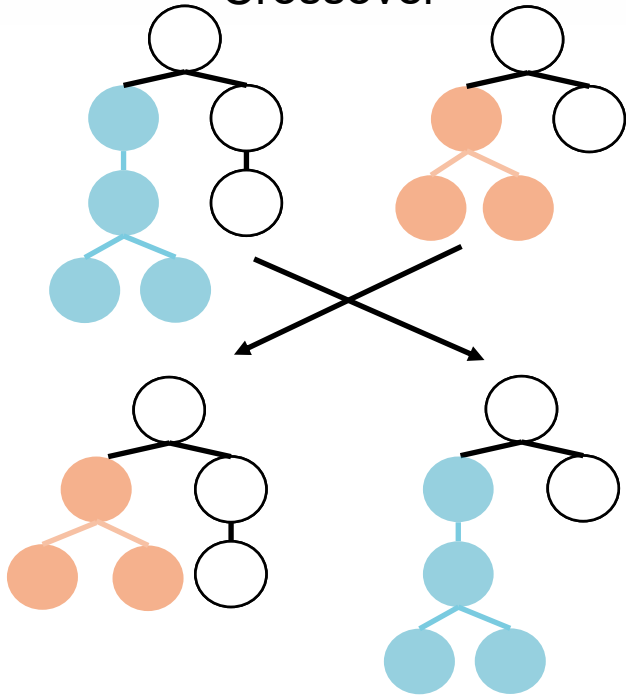
Function

Program

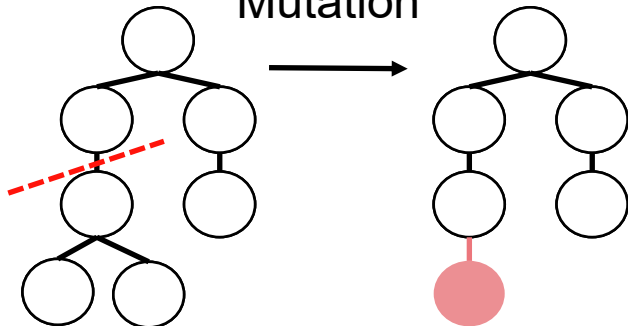
- Recombitment strategies are programs
- Programs have traits that can be evolved
- Why Evolutionary learning ?
  - Learning is an optimization problem
  - Learning  $\Leftrightarrow$  Recognizing
- “**Strategies** with **traits** that enable them to improve the Investment Degree will help them survive and **have more offspring**, which will inherit those **traits**.”

# How do we evolve program ?

Crossover



Mutation



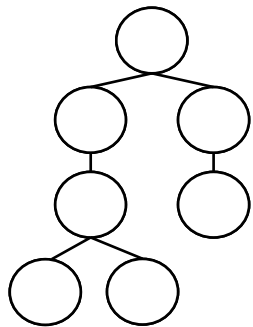
- Program  $\Leftrightarrow$  Hierarchical Data structure
- Abstract Syntax Tree (AST)
- Two main operators:
  - Crossover – exploitation
  - Mutation – exploration
- The best individual will survive?
- How do you measure it ?

# How to measure the fitness ?

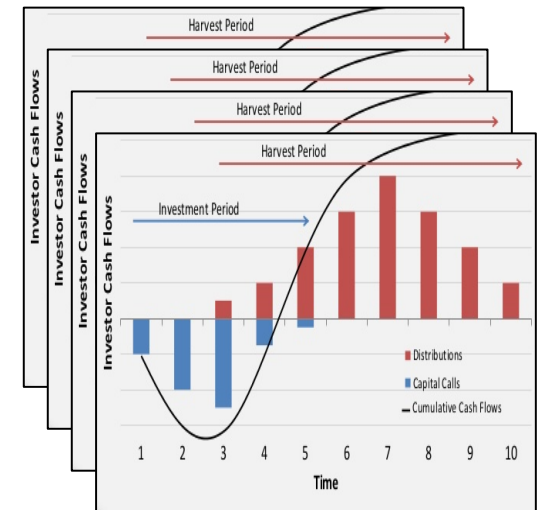
## Program

## Function

## Recommitment Strategy

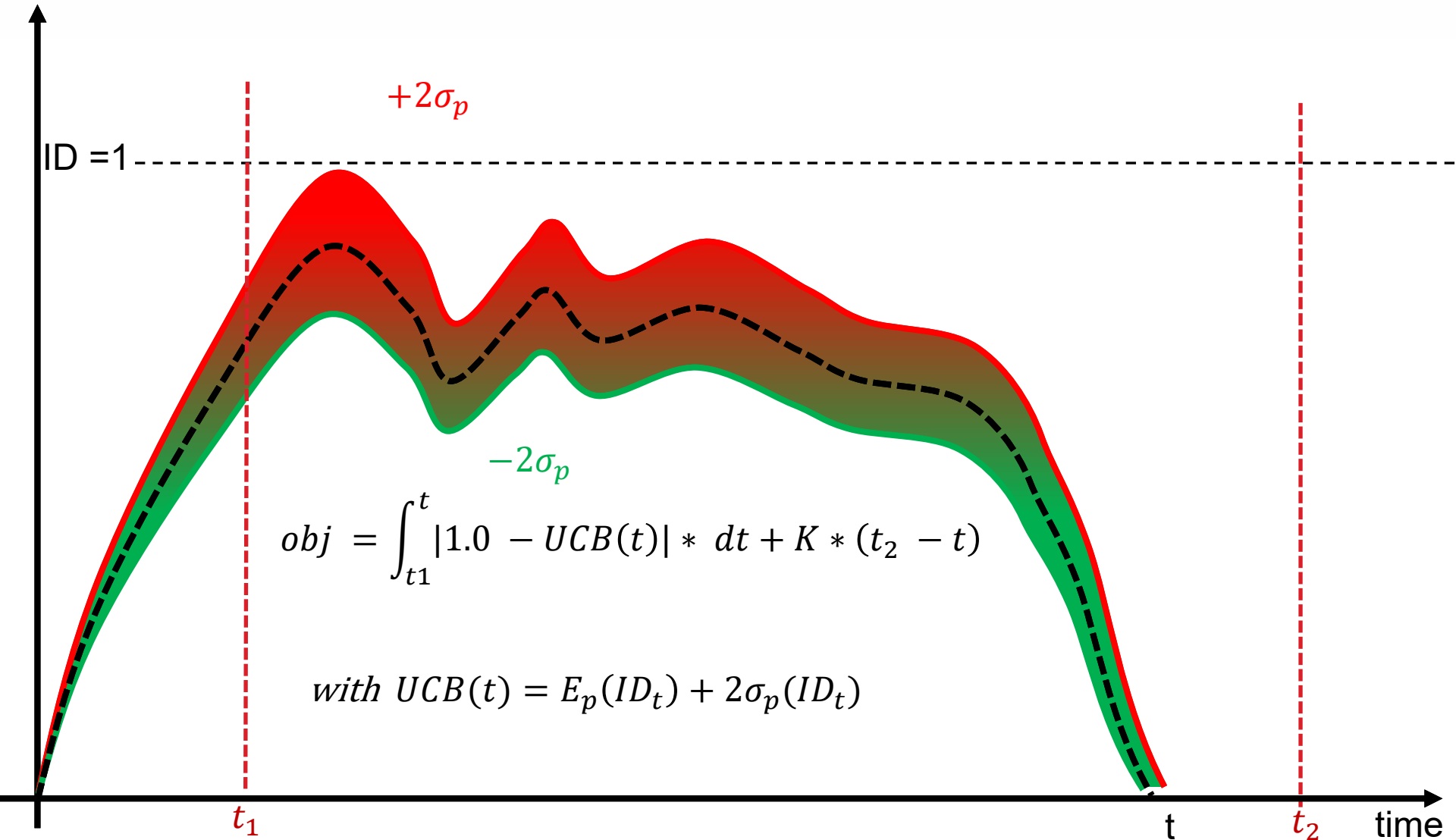


$$C_t = \frac{1}{ID_t} (D_t + UC_{t-p})$$



Name	Description
<i>Operators</i>	
+	Add two inputs
-	Subtract two inputs
*	Multiply two inputs
%	Divide two inputs with protection
min	Minimum b.t.w. two inputs
max	Maximum b.t.w. two inputs
<i>Terminal sets/ Arguments</i>	
$C_t$	Contributions at $t$
$D_t$	Distributions at $t$
$ID_t$	Investment degree at $t$
$NAV_t$	Net Asset Value at $t$
$error_t$	Deviation to ideal ID at $t$
$DZ^3(t)$	deZwart's strategy n°3 [8] at $t$
$UC_{t-24}$	Uncalled capital for commitments made 24 quarters ago
$CCommit_{t-24}$	Capital committed for 24 quarters

# How to measure the fitness ?



- Artificial cashflows:
  - PE players protect their rich data histories
  - Private market data providers generally sell data
  - Cover very specific periods and incomplete
  - Synthetic cashflows generated from a stochastic version of the Yale Model

## Genetic Programming parameters

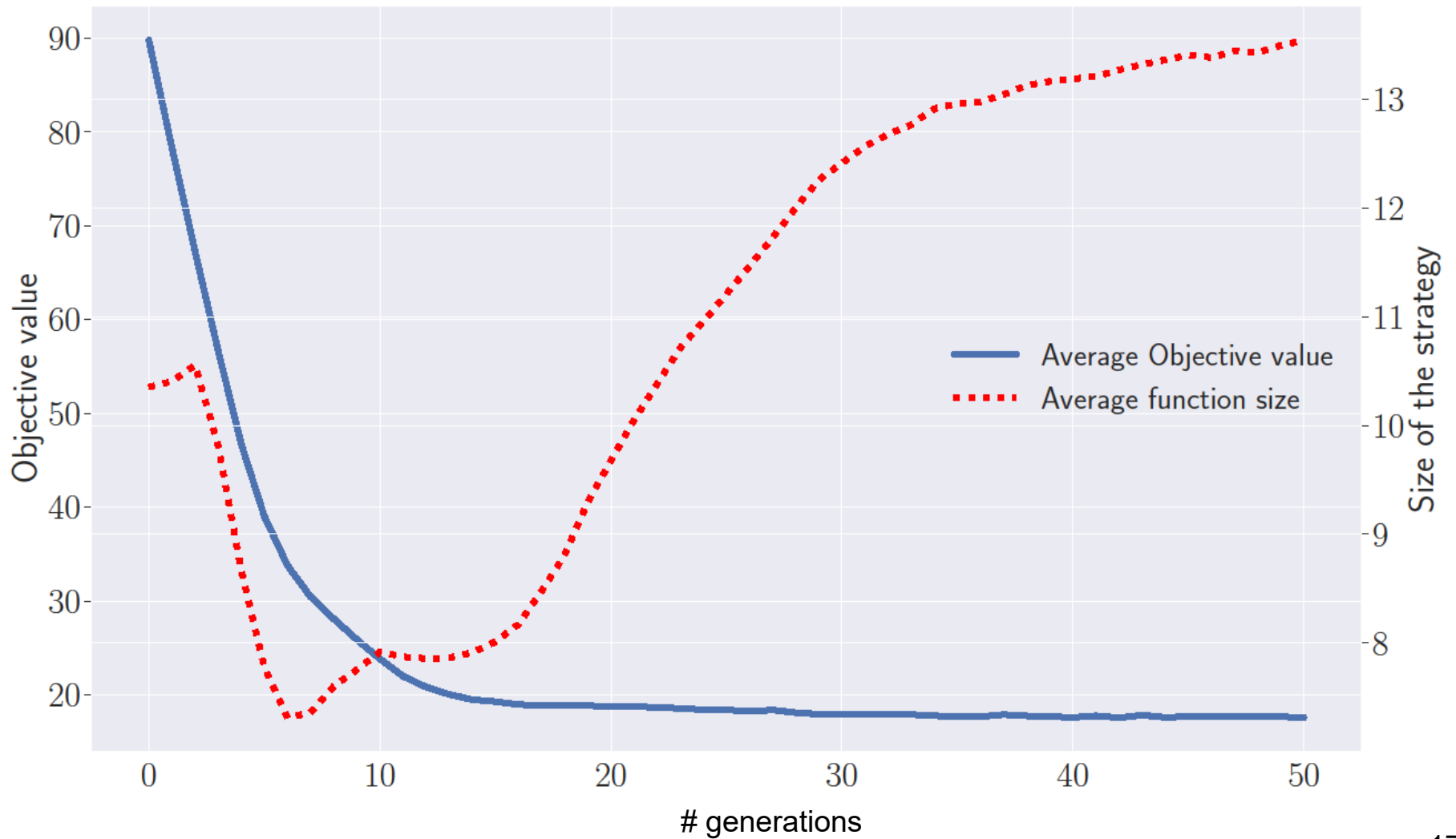
<b>Runs</b>	30
<b>Generations</b>	50
<b>Population size</b>	500
<b>Crossover Probability (CXPB)</b>	0.85
<b>Mutation Probability (MUTPB)</b>	0.1
<b>Reproduction Probability</b>	0.05
<b>Tree initialization method</b>	Ramped half-and-half
<b>Selection Method</b>	Tournament selection with size=7
<b>Depth limitation</b>	17
<b>Crossover Operator (CX)</b>	One crossover point
<b>Mutation Operator (MUT)</b>	Grow

## Simulation parameters

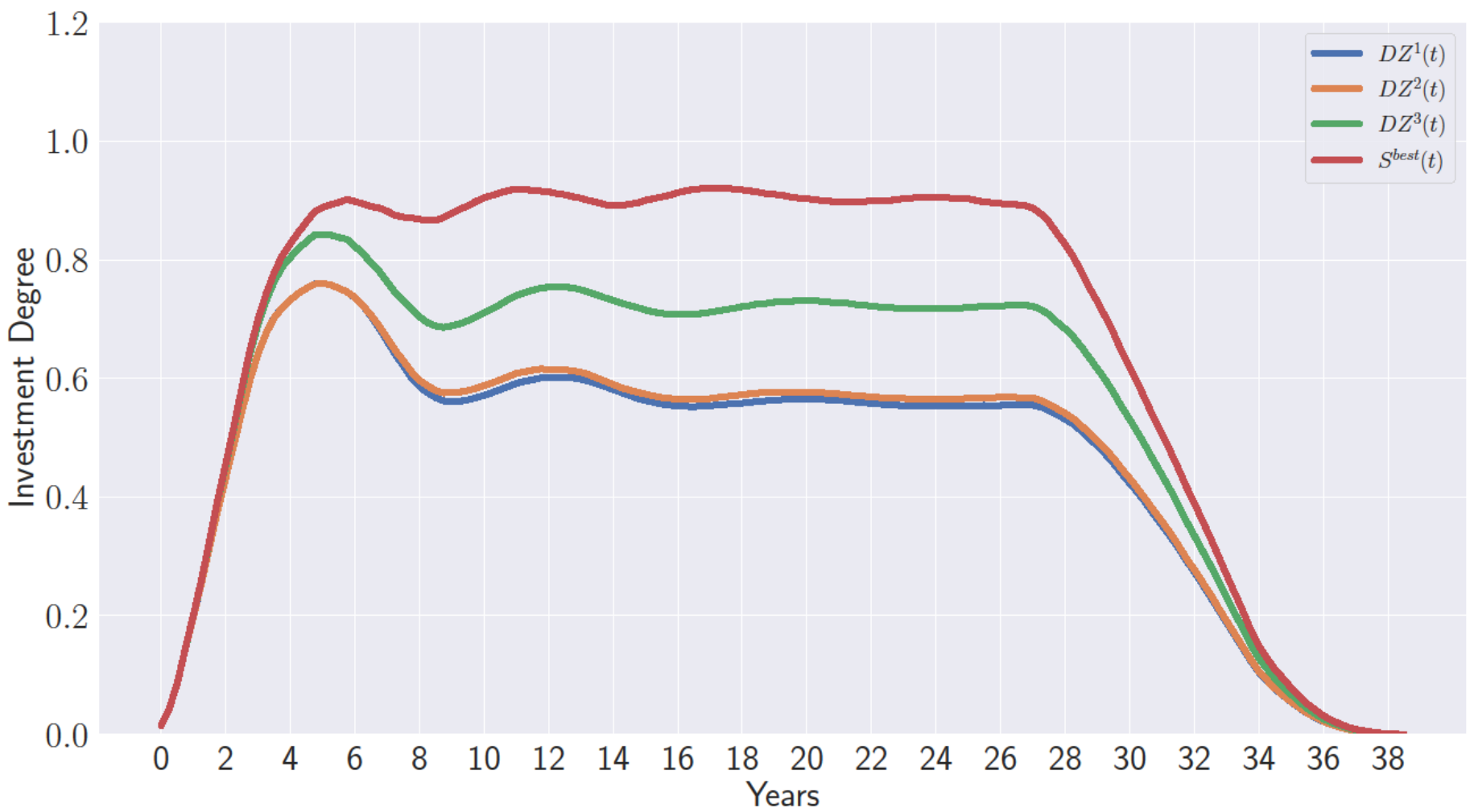
<b>Parameters</b>	<b>Training</b>	<b>Validation</b>
<b>Cashflows frequency</b>	quarterly	quarterly
<b>Investment period</b>	26 years	26 years
<b>Funds per recommitment</b>	4	4
<b>Fund selection</b>	ESG score	ESG score
<b>Number of simulated portfolios (per evaluation)</b>	250	1000
<b>Distributed simulation</b>	True	False



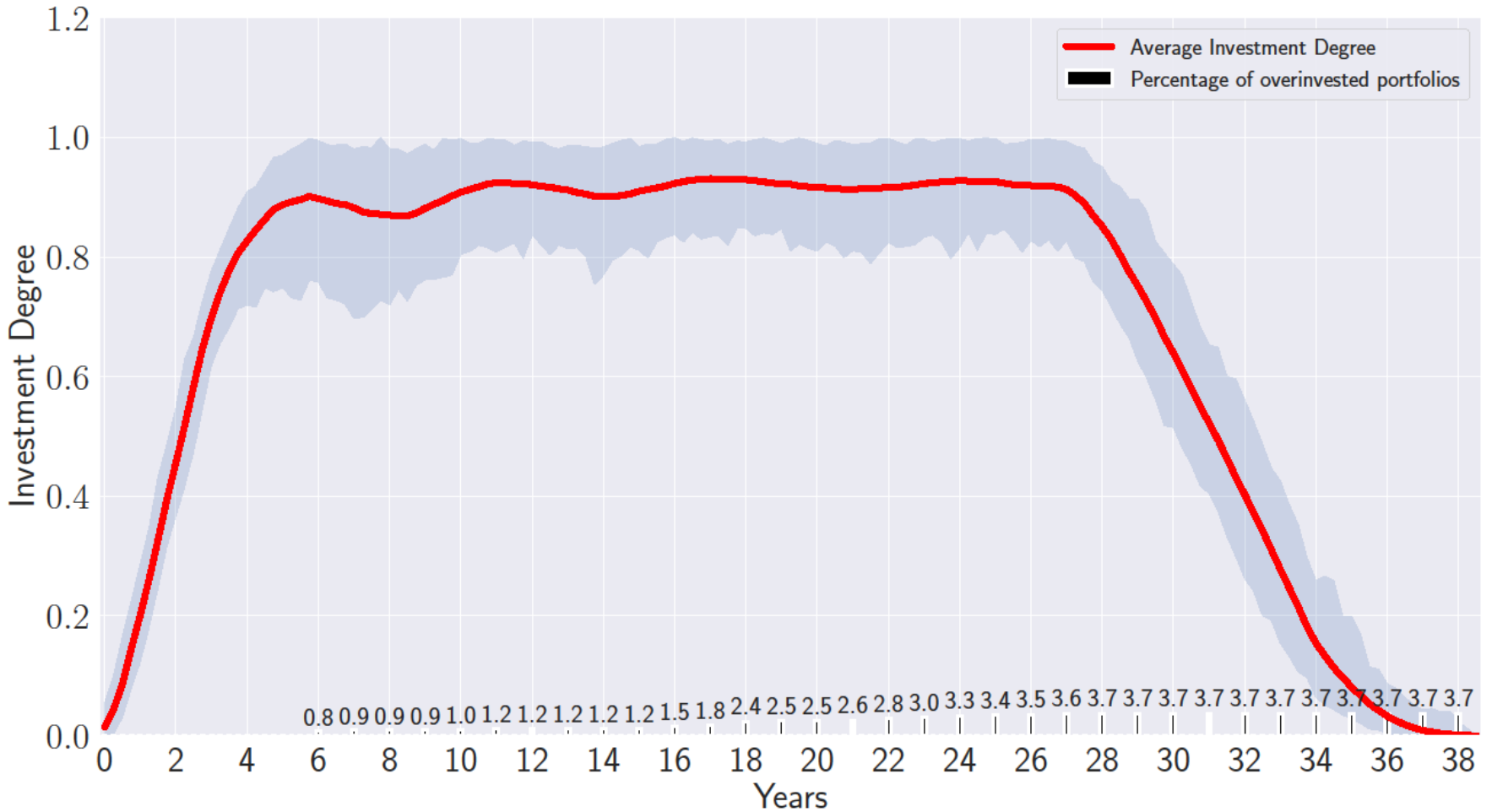
# Experimental results



# Experimental results



# Experimental results



Best strategy obtained from the 30 runs, i.e.,  $S^{best}(t) =$

$$\max(-Cash_t \times D_t + DZ^3(t), \min(Cash_t, D_t + 2UC_{t-24})) +$$

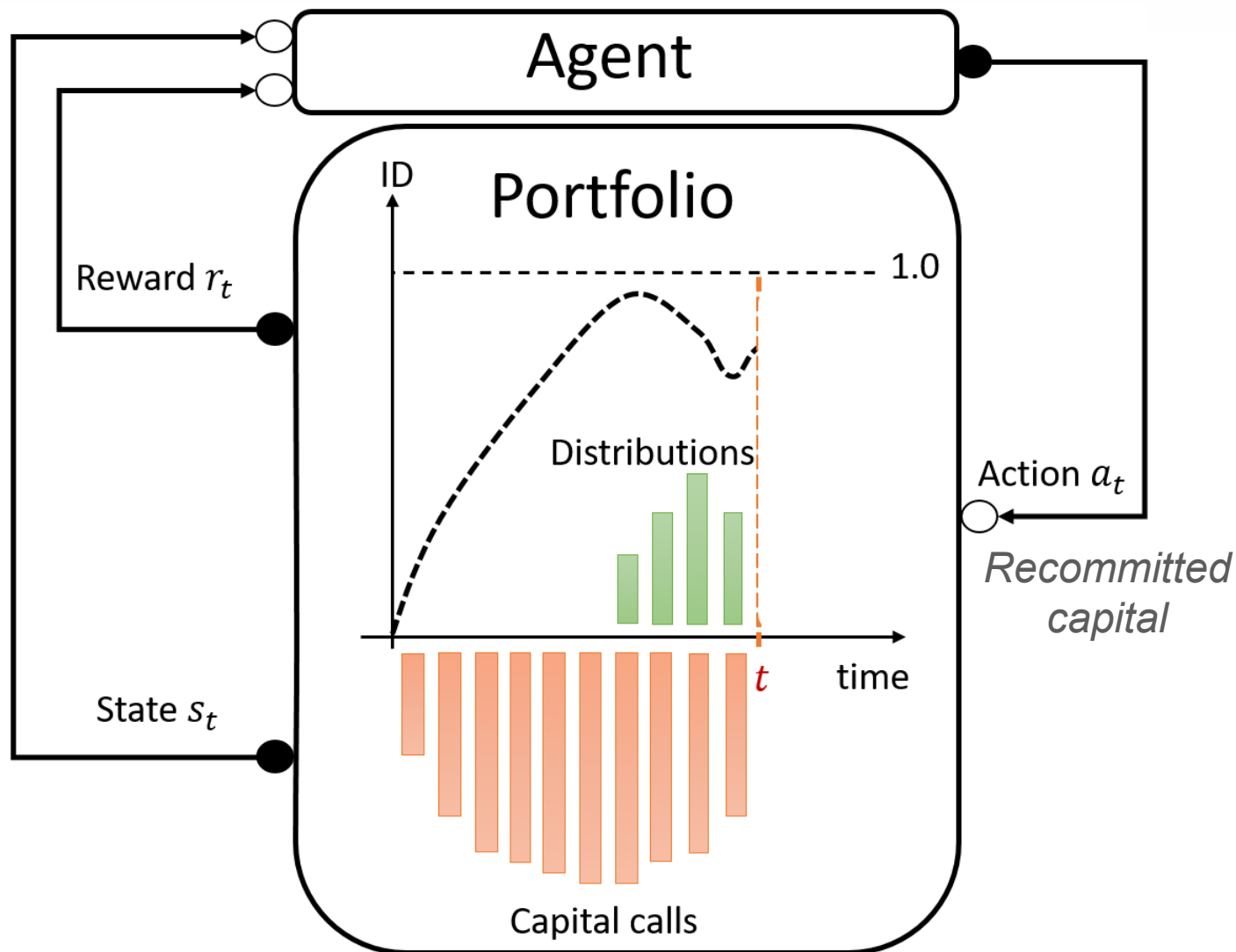
$$\min(Cash_t, \max(D_t^2, D_t + 2UC_{t-24}))$$

# Proximal Policy Optimisation for a Private Equity Recommitment System

# Learning Recombitment policies

- Using a policy-based algorithm  $\sim$  Proximal Policy Optimization (PPO)
- Target recommitment policies maintaining an Investment Degree close to 1
- Policy-based VS Value-based:
  - Avoid computational burden to compute all state-values
  - Action space is continuous
- Drawbacks:
  - On-policy approaches
  - Large number of simulations

# RL model of the PE recommitment problem



# RL model of the PE recommitment problem

- State  $s_t = \langle ID_t, D_t, CC_t, UC_{t-24}, Cash_t, NAV_t \rangle$ 
  - Portfolio state
  - Important features to recommit
- Continuous action  $a_t \Rightarrow$  capital recommitted into new PE funds

- Final reward  $\underbrace{\sum_{t=1}^T ID_t \times 10^{(digits(T)+1)}}_{\text{Global reward}} + \underbrace{\sum_{t=1}^T r_t^{valid}}_{\text{Local reward}}$

Global reward:

- Based on ID
- Only if no cash shortage

Local reward:

- $r_t^{valid} = \begin{cases} 0 & \text{if } ID_t > 1 \\ 1 & \text{else} \end{cases}$

- Create a different order of magnitude between valid portfolios and invalid ones (constraint handling)
- Accumulated local reward + shifted global reward

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## Algorithm 1 PPO-clip version

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- 1: Initialize policy parameters  $\theta_1$  and value function parameters  $\phi_1$
- 2: **for**  $k \in \{1, \dots, M\}$  **do**
- 3:   Sample a set of trajectories  $\{\tau_i\}_{i=1}^M$  using the policy  $\pi_{\theta_k}$
- 4:   Create a batch  $\mathcal{B}$  of transitions  $(s_t^i, a_t^i, r_t^i) \forall t \in \{1, \dots, |\tau_i|\} \forall i \in \{1, \dots, M\}$
- 5:   Compute rewards-to-go  $\hat{\mathcal{R}}_t^i$ , i.e. rewards from action  $a_t^i$ ,  $\forall t \in \{1, \dots, |\tau_i|\} \forall i \in \{1, \dots, M\}$
- 6:   Estimate the advantages  $A^{\pi_{\theta_k}}(s_t^i, a_t^i)$  using the value function  $V_{\phi_k}$
- 7:   Perform policy update:

$$\theta_{k+1} = \arg \max_{\theta} \frac{1}{M} \sum_{i=1}^M \frac{1}{|\tau_i|} \sum_{t=1}^{T_i} \left[ \min \left( A^{\pi_{\theta}}(s_t^i, a_t^i) \frac{\pi_{\theta}(a_t^i | s_t^i)}{\pi_{\theta_{old}}(a_t^i | s_t^i)}, g(\epsilon, A^{\pi_{\theta}}(s_t^i, a_t^i)) \right) \right]$$

$$\text{with } g(\epsilon, A^{\pi_{\theta}}(s_t^i, a_t^i)) = \text{clip} \left( \frac{\pi_{\theta}(a_t^i | s_t^i)}{\pi_{\theta_{old}}(a_t^i | s_t^i)}, 1 - \epsilon, 1 + \epsilon \right)$$

- 8:   Perform value function update by minimizing mean-squared error:

$$\phi_{k+1} = \arg \min_{\phi} \frac{1}{M} \sum_{i=1}^M \frac{1}{|\tau_i|} \sum_{t=1}^{T_i} \left[ V_{\phi}(s_t^i) - \hat{\mathcal{R}}_t^i \right]^2$$

- 9: **end for**
-



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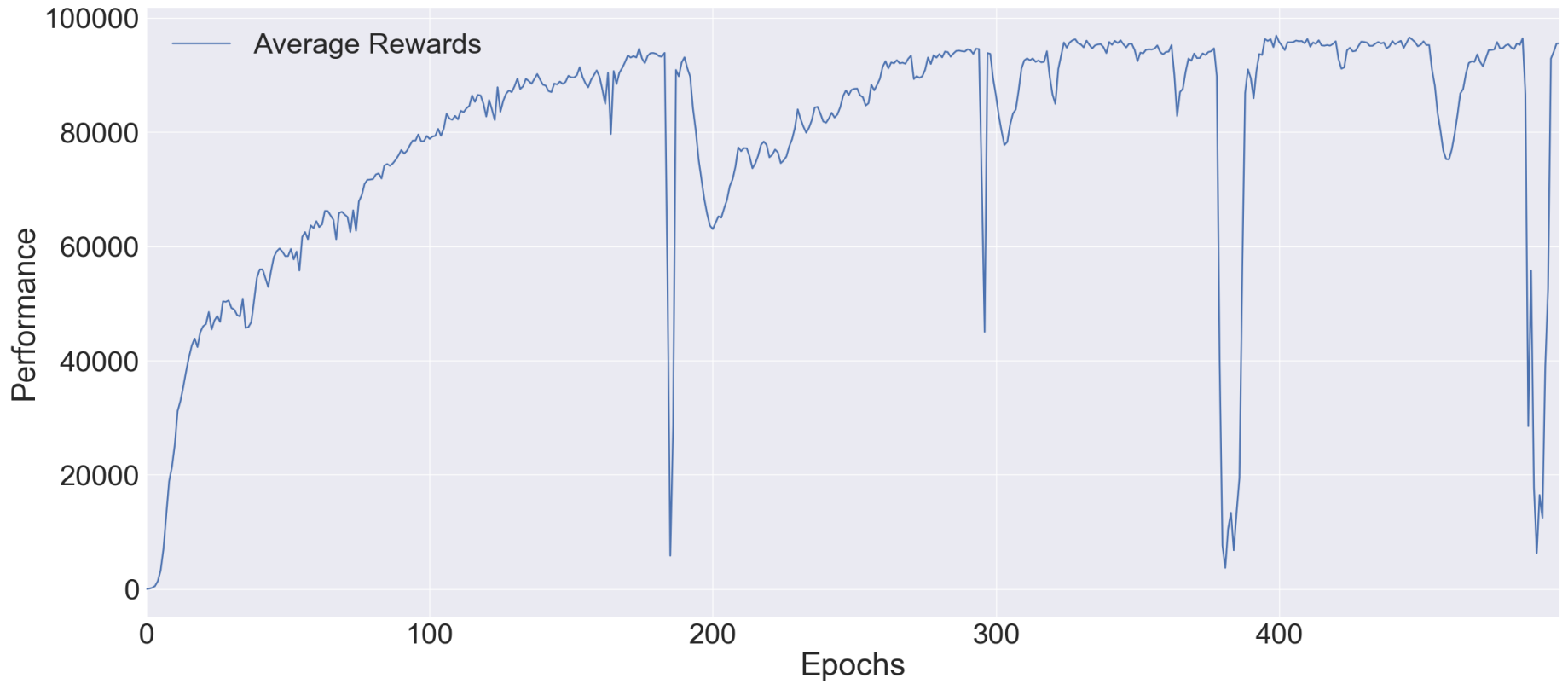
## RL parameters

Parameters	Value
steps_per_epoch	26000
gamma	1
epochs	500
# episodes	125000
clip_ratio $\epsilon$	0.2
pi_lr / vf_lr	$3e^{-4} / 1e^{-4}$
hidden layers	[64, 64]

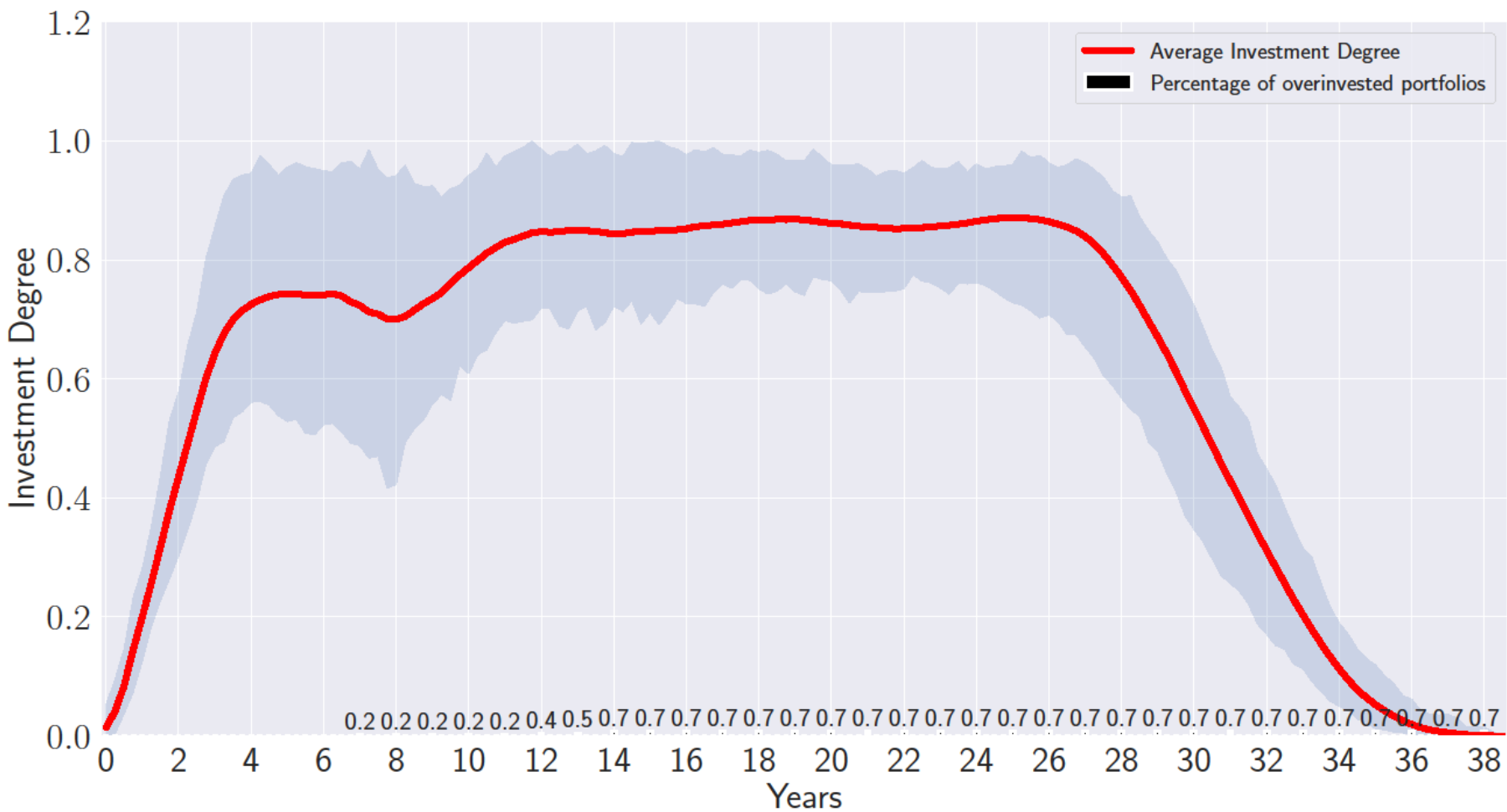
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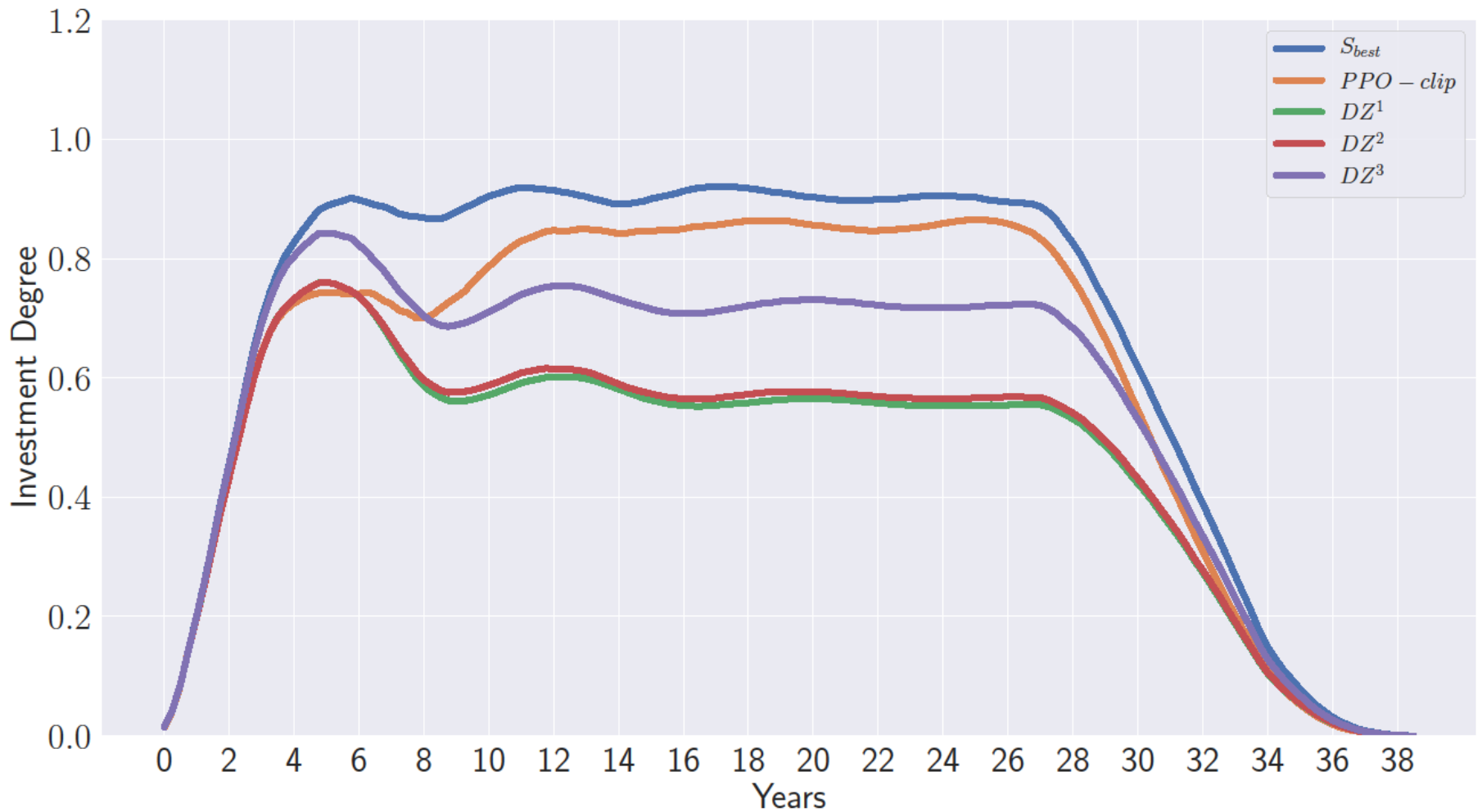
# Rewards evolution



# Best policy obtained with PPO-clip



# Comparison with existing strategies



- Strong influence in today's financial marketplace
- PE challenges:
  - Stakes in PE are illiquid due to restriction on sales
  - Exposure to PE by investing in new funds in which they **commit**
  - Capital is drawn down **gradually** over several years
  - Very often Capital is not **entirely** called
  - Most of these distributions cannot be reinvested immediately and are **recommitted** to new PE funds
- Efficient recommitment policies/rules can be generated using Reinforcement Learning
- Next steps:
  - Multi-objective Reinforcement Learning
  - Multi-class assets portfolios

# What's next ?

# Providing a set of alternatives

- When liquidity is soft constraint
- Multi-class asset portfolios

Pareto front: Investment Degree vs Injected Cash



**Thank you for your attention**